

ELEKTRIKA:

$$I = \frac{de}{dt}$$

$$\int I \cdot dt = \Delta e$$

$$F = \frac{e_1 e_2}{4\pi\epsilon_0 r^2} = e_0 \frac{E}{r^2}$$

$$U = E \cdot s = \frac{A_e}{e}$$

$$\sigma_e = \frac{e}{S}$$

$$E = \frac{\sigma}{2\epsilon_0}$$

$$\oint D dS = e$$

$$e = CU, \dots, e_p = CU_p$$

$$C = \frac{\epsilon_0 S}{l \ln r_2 / r_1} = \frac{2\pi\epsilon l}{\ln r_2 / r_1}$$

$$W_e = \frac{CU^2}{2} = \frac{e^2}{2C}$$

$$W_p = qV$$

$$\Delta W_p + \Delta W_{kin} = 0$$

$$w_e = \frac{W_e}{V} = \frac{\epsilon_0 E^2}{2}$$

$$U = RI$$

$$P = UI = RI^2 = \frac{U^2}{R}$$

$$R = \frac{\xi \cdot l}{S_0}$$

$$A = \int F \cdot ds = \int Md\varphi = \int Pdt = \Delta W$$

$$U_g = U_0 - IR_n$$

$$I_k = \frac{U_0}{R_n}$$

$$Q = A = \int U \cdot de = \int U \cdot I \cdot dt = \int RI^2 \cdot dt = \int I^2 R dt$$

$$Q = m \cdot c \cdot \Delta T$$

Kapacitivnosti:
- naelektrena ploskev

$$C = \frac{\epsilon A}{d}$$

- valjasti kondenzator (koaks)

$$C = \frac{2\pi\epsilon l}{\ln \frac{r_2}{r_1}}$$

- kroglasti kondenzator:

$$C = \frac{4\pi\epsilon r_1 r_2}{r_2 - r_1}$$

Praznjenje kondenzatorja:

$$U_c = U_0 \cdot e^{-\frac{t}{RC}}$$

$$I_c = I_0 \cdot e^{-\frac{t}{RC}}$$

Polnjenje kondenzatorja:

$$U_c = U_g (1 - e^{-\frac{t}{RC}})$$

$$I_c = \frac{U_g}{R} e^{-\frac{t}{RC}}$$

Admitanca kondenzatorja:

$$Z_C = \frac{1}{\omega C}$$

RLC vezje:

$$U_0 = I \cdot \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

Krožna zanka:

$$V = \frac{e}{4\pi\epsilon_0 \sqrt{r^2 + z^2}}$$

$$E = \frac{e \cdot z}{4\pi\epsilon_0 (r^2 + z^2)^{3/2}}$$

MAGNETIZEM:

$$F = IBl \cdot \sin \alpha$$

$$F = e \cdot v \times B$$

$$B = \mu_0 H = \frac{\mu_0 I}{2\pi r} = \frac{\mu_0 NI}{l}$$

$$M = NISB \sin \alpha = J\alpha$$

$$U_i = \frac{d\Phi_m}{dt} = -BS\omega \cdot \sin(\alpha t) = \dot{v} \cdot (B \times \dot{r})$$

$$\Phi_m = \int BdS = BS \cdot \cos(\alpha t) = [Vs]$$

$$d\Phi_m = SdB$$

$$L = \frac{\mu_0 N^2 S}{l} = \frac{\Phi}{I}$$

$$W_m = \frac{LI^2}{2} = p_m B \cos \varphi$$

$$p_m = NIS$$

$$w_m = \frac{B^2}{2\mu_0} = \frac{HB}{2}$$

Biot-Savartov zakon:

$$dB = \frac{\mu_0 I (r \times dl)}{4\pi r^3}$$

Nihajni čas mag. igle ali tuljave

p_m - mag. moment

$$t_0 = 2\pi \sqrt{\frac{J}{p_m B}}$$

Zakon o mag. pretoku:

$$\oint B dS = 0$$

Zakon o mag. napetosti (Amperov zakon):

$$\oint H \cdot dS = I$$

$$B = \mu_0 H$$

H okoli vodnika in dolge tuljave:

$$H = \frac{I}{2\pi r} = \frac{NI}{l}$$

Pojemanje toka in napetosti skozi tuljavo:

$$\tau = L/R$$

$$I(t) = I_0 \cdot e^{-t/\tau}$$

$$U_R = -I_0 \cdot R \cdot e^{-t/\tau}$$

$$U_L = I_0 \cdot R \cdot e^{-t/\tau}$$

Naraščanje toka in napetosti skozi tuljavo:

$$I(t) = \frac{U_0}{R} (1 - e^{-t/\tau})$$

$$U_R = -U_0 (1 - e^{-t/\tau})$$

$$U_L = -U_0 \cdot e^{-t/\tau}$$

Impedanca tuljave:

$$Z_L = \omega L$$

Izmenični tok:

$$I_{ef} = \sqrt{\frac{1}{T} \int_0^T I^2 \cdot dt} = \frac{I_0}{\sqrt{2}}$$

$$U_{ef} = \sqrt{\frac{1}{T} \int_0^T U^2 \cdot dt} = \frac{U_0}{\sqrt{2}}$$

$$I = I_0 \cdot \sin(\omega t)$$

$$U = U_0 \cdot \sin(\omega t + \delta)$$

Električni nihajni krog:

Idealni: (tuljava, kondenzator → zaporedno)

$$\frac{e}{C} - L \frac{dI}{dt} = 0 - \text{kirchoff}; I = -\frac{de}{dt}$$

$$\frac{d^2 e}{dt^2} + \frac{1}{LC} e = 0 - \text{diferencia ln a}$$

Re šitev:

$$e(t) = e_0 \cdot \cos \omega_0 t$$

$$\omega_0 = \sqrt{\frac{1}{LC}};$$

$$I(t) = \omega_0 \cdot C \cdot U_0 \cdot \sin \omega_0 t$$

$$W_C = \frac{e^2}{2C} = \frac{CU_0^2}{2} \cos^2 \omega_0 t$$

$$W_L = \frac{LI^2}{2} = \frac{CU_0^2}{2} \sin^2 \omega_0 t$$

$$W_C + W_L = \frac{CU_0^2}{2}$$

Z dušenjem: (kondenzator tuljava, upor → zaporedno)

$$\frac{e}{C} - IR - L \frac{dI}{dt} = 0 - \text{kirchoff}; I = -\frac{de}{dt}$$

$$\frac{d^2 e}{dt^2} + \left(\frac{R}{L}\right) \cdot \frac{de}{dt} + \left(\frac{1}{LC}\right) e = 0 - \text{diferen}$$

Re šitev:

$$e(t) = e_0 \cdot e^{-\beta t} \cdot \cos \omega' t$$

$$\beta = \frac{R}{2L}$$

$$\omega' = \sqrt{\omega_0^2 - \beta^2}$$

$$\omega_0 = \sqrt{\frac{1}{LC}};$$

Vsiljeno nih.: (tuljava, kondenzator upor, generator → zaporedno)

$$I(t) = I_0 \cdot \sin \omega t$$

$$U_G = U_0 \cdot \sin(\omega t + \delta)$$

$$U_0^2 = (U_L - U_C)^2 + U_R^2$$

$$U_R = R \cdot I_0$$

$$U_C = \left(\frac{1}{\omega C} \right) \cdot I_0$$

$$U_L = (\omega \cdot L) \cdot I_0$$

$$I_0 = \frac{U_0}{\sqrt{(\omega \cdot L - \frac{1}{\omega \cdot C})^2 + R^2}} = \frac{U_0}{Z}$$

Fazni _ premik :

$$\text{tg} \delta = \frac{U_L - U_C}{U_R} = \frac{\omega \cdot L - \left(\frac{1}{\omega \cdot C} \right)}{R}$$

Če _ je : ($\omega = \omega_0$) je ($\delta = 0$) in _ je :

$$\bar{P} = U_{EF} \cdot I_{EF} \cdot \cos \delta \rightarrow \text{maksima ln } a$$

Mg. Polje tč. naboja:

$$B = \frac{v \times E}{c^2}$$

Mg polje ravnega vodnika:

$$B = \frac{\mu_0 I}{2\pi a}$$

Mg polje v dolgi ravni tuljavi:

$$B = \frac{\mu_0 NI}{l}$$

Mg polje v svitku:

$$B = \frac{\mu_0 NI}{2\pi r}$$

Zakon o el. nap. (Faradejev zakon):

$$\int E \cdot ds = - \frac{d(\int B \cdot dS)}{dt}$$

Induktivnost:

$$\Phi_m = L \cdot I \text{ - lastna induktivnost}$$

$$L = \frac{\mu_0 NS^2}{l} \text{ Dolga ravna tuljava}$$

$$L = \frac{\mu_0 N^2 h \ln(b/a)}{2\pi} \text{ Svitek}$$

$$L = \frac{\mu_0 l \cdot \ln(b/a)}{2\pi} \text{ Koaks}$$

$$U_i = - \frac{L \cdot dl}{dt} \text{ v smeri toka velja}$$

Magnetna upornost:

$$R_m = \frac{l}{\mu_r \mu_0 \cdot S}$$

SEVANJE:

a - albedo ali odbojnost

j - gostota energ. Toka.

$$P_{ABS} = (1 - a) j S$$

$$P_{IZS} = (1 - a) \sigma T^4 S$$

C - toplotna kapaciteta [J/K]

$$-dQ = j^* S dt$$

$$-CdT = \sigma T^4 S dt$$

- Stefanov zakon (sevanje črnega telesa):

$$\lambda_m \cdot T = k_w$$

$$j_{\epsilon}^* = \sigma \cdot T^4$$

- λ_m - val. dolžina. pri kateri telo največ seva

- $k_w = 2.9 \text{ mm}$

FOTOMETRIJA:

Svetlobni tok:

$$P = \frac{dW}{dt} = [W]$$

Gostota svetlobnega toka:

$$j = \frac{dP}{dS} = \frac{P}{4\pi r^2} = \left[\frac{W}{m^2} \right]$$

Svetilnost:

$$I = \frac{dP}{d\Omega} = \left[\frac{W}{sr} = \frac{lm}{sr} = cd \right]$$

$$I = r^2 \cdot j = BS_0 \cos \varphi$$

$$dI = B \cdot dS \cdot \cos \vartheta$$

Svetlost:

$$B = \frac{dI}{dS_0} = \left[\frac{W}{sr \cdot m^2} = \frac{cd}{m^2} = nit \right]$$

Osvetljenost:

$$E = \frac{dP}{dS} = \left[\frac{W}{m^2} = \frac{lm}{m^2} = lx \right]$$

$$E = j \cdot \cos \varphi$$

$$dE = \frac{dI \cdot \cos \vartheta}{r^2}$$

GEOMETRIJSKA OPTIKA:

Odboj in lom svetlobe:

Lomni količnik:

$$n = c_0 / c$$

Lomni zakon:

$$n_1 \sin \alpha = n_2 \sin \beta$$

Totalni odboj:

$$\sin \beta_t = \frac{n_1}{n_2}$$

Gorišče:

f - goriščna razdalja

a - razdalja predmeta od zrcala

b - razdalja slike od zrcala

d - dioptrija

$$\frac{1}{f} = \frac{1}{a} + \frac{1}{b}$$

$$d = a + b = a_1 + a_2 = b_1 + b_2$$

Gor. razdalja zbiral. krogelnega zrcala:

r - radij krogle ali krivinski polmer

$$f = \frac{r}{2}$$

Povečava:

$$N = b / a$$

Bikonveksna leča:

$$\frac{1}{f_1} = \left(\frac{n}{n_1} - 1 \right) \frac{2}{r}$$

Sestavi nerazmaknjenih leč:

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2}$$

1/f - lomnost; enota je dioptrija [1/m]

Povečava lupe:

α - kot pod katerim vidimo predmet z lupo

α_0 - kot pod katerim vidimo predmet z prostim očesom

$$N = \frac{\tan \alpha}{\tan \alpha_0} = \frac{a_0}{f}$$

Povečava mikroskopa:

f - gorišče objektivna

f' - gorišče okularja

x' - razdalja med goriščema (tubus)

a_0 - normalna zorna razdalja

$$N = \frac{\tan \alpha}{\tan \alpha_0} = \frac{a_0 \cdot x'}{f \cdot f'}$$

$$\tan \alpha_0 = \frac{y}{a_0}$$

$$\frac{y'}{y} = \frac{b}{a}, \text{ ,, } \tan \alpha = \frac{y'}{f_2}$$

Daljnogled:

$$N = \frac{\tan \alpha}{\tan \alpha_0} = \frac{f}{f'}$$

Daljnovidnost:

-zbiralna leča

$$\frac{1}{f_{\min}} = \frac{1}{a_{\min}} + \frac{1}{b}$$

$$\frac{1}{a_0} + \frac{1}{b} = \frac{1}{f_{\min}} + \frac{1}{f_{\text{očča}}}$$

$$f_{\text{očča}} = \frac{a_0 \cdot a_{\min}}{a_{\min} - a_0}$$

Kratkovidnost:

-razpršilna leča

$$\frac{1}{f_{\max}} = \frac{1}{a_{\max}} + \frac{1}{b}$$

$$\frac{1}{\infty} + \frac{1}{b} = \frac{1}{f_{\max}} + \frac{1}{f_{\text{očča}}}$$

$$f_{\text{očča}} = -a_{\min}$$

POSEBNA TEORIJA RELATIVNOSTI

Transformacija za hitrosti:

$$v'_x = \frac{v_x - v_0}{\left(1 - \frac{v_0 v_x}{c_0^2} \right)}$$

$$v'_y = \frac{v_y}{\gamma_0 \left(1 - \frac{v_0 v_x}{c_0^2} \right)}$$

$$v'_z = \frac{v_z}{\gamma_0 \left(1 - \frac{v_0 v_x}{c_0^2} \right)}$$

Obratna transformacija:

$$v_x = \frac{v'_x + v_0}{\left(1 + \frac{v_0 v'_x}{c_0^2}\right)}$$

$$v_y = \frac{v'_y}{\gamma_0 \left(1 + \frac{v_0 v'_x}{c_0^2}\right)}$$

$$v_z = \frac{v'_z}{\gamma_0 \left(1 + \frac{v_0 v'_x}{c_0^2}\right)}$$

Skrčenje dolžin:

Palica miruje v sistemu S:

$$x_2 - x_1 = L$$

Dogodek 1:

$$t_1 = 0 \quad x_1 = 0$$

Dogodek 2:

$$t_2 = \frac{v_0 L}{c_0^2} \quad x_2 = L$$

Lorentzova transformacija

Sistem S':

Dogodek 1:

$$t'_1 = 0 \quad x'_1 = 0$$

Dogodek 2:

$$t'_2 = 0 \quad x'_2 = \frac{L}{\gamma_0}$$

$$x'_2 - x'_1 = \frac{L}{\gamma_0} = L'$$

Podaljšanje časa

1. dogodek: mesto x, čas t₁

2. dogodek: mesto x, čas t₂

$$\Delta t = t_2 - t_1$$

Lorentzova transformacija:

$$t'_1 = \gamma_0 \left(t_1 - \frac{v_0 x}{c_0^2} \right)$$

$$t'_2 = \gamma_0 \left(t_2 - \frac{v_0 x}{c_0^2} \right)$$

$$t' = t'_2 - t'_1 = \gamma_0 (t_2 - t_1) = \gamma \tau$$

$$\Delta t' = \gamma_0 \Delta t$$

$$t_1 = \gamma \left(t'_1 + \frac{v \cdot x'_1}{c^2} \right)$$

$$t_2 = \gamma \left(t'_2 + \frac{v \cdot x'_2}{c^2} \right)$$

$$x'_1 = \gamma (x_1 - vt_1)$$

$$x'_2 = \gamma (x_2 - vt_2)$$

$\Delta t' \geq \Delta t \Rightarrow$ za gibajočega opazovalca dogodki

potekajo počasneje kot za opazovalca, ki miruje ob dogodkih.

ZAKONI GIBANJA

Gibanje delca

dt – čas, ki ga izmeri opazovalec, ki opazuje gibanje

točkastega telesa

dτ – lastni čas, ki ga izmeri opazovalec, ki se giblje skupaj z

delcem

$$dt = \gamma d\tau$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}, \dots, \gamma^2 = \frac{v^2 \gamma^2}{c^2} + 1$$

$$v = \sqrt{1 - \frac{1}{\gamma^2}} \cdot c$$

GIBALNA KOLIČINA

E – polna energija

m₀ ali mc² – mirovna masa

p – gibalna količina

$$E = mc^2 = \left[\frac{eV}{c^2} \right]$$

$$E = W_k + m_0 c^2$$

$$E = \sqrt{p^2 c^2 + m_0^2 c^4}$$

$$W_k = mc^2 (\gamma - 1) = [eV]$$

$$p = \gamma mv = e_0 Et = \left[\frac{eV}{c} \right]$$

$$p = \sqrt{\frac{W_k^2 + 2W_k m_0 c^2}{c^2}}$$

De Brogliejeva val dolžina:

Fotoni:

$$P = t \cdot k = \frac{h}{\lambda}$$

$$W = t \cdot \omega$$

$$t = \frac{h}{2\pi}$$

$$k = \frac{2\pi}{\lambda}$$

Elektroni:

$$\lambda_B = \frac{h}{P} = \frac{h}{m \cdot v}$$

OSTALO:

-Sevanje črnega telesa

$$E = mc^2$$

$$E = 4\pi r^2 \sigma T^4 \cdot t - \text{okroglo_telo(sonce)}$$

-Fotoni

$$W_\gamma = h\nu = \frac{hc}{\lambda}$$

$$I = \frac{de}{dt} = \frac{d(N_e \cdot e_0)}{dt} \Rightarrow N_e = N_\gamma / 20$$

$$P = \frac{dW}{dt} = \frac{d(N_\gamma \cdot h\nu)}{dt}$$

-Sevanje žičke

$$P_{el} = P_{iz}$$

$$I^2 R = \sigma T^4 S$$

$$R = \frac{\xi \cdot l}{\pi \cdot r^2}$$

$$S = 2\pi r l \rightarrow S_žice$$

-Leče in lomni količniki

$$\frac{1}{f_1} = \left(\frac{n}{n_1} - 1 \right) \frac{2}{R}$$

-Svetloba

$$P_s = f \cdot \int \frac{dP}{d\lambda}(\lambda) \cdot \eta_{rbo} \cdot d\lambda$$

$$f = 683 \frac{lm}{W}$$

$\eta_{rbo}(\lambda = nm)$:

$\lambda < -\infty - 1 \Rightarrow$ žarki x

$\lambda = 1 - 380 \Rightarrow$ UV svetloba

$\lambda = 380 - 396 - 439 \Rightarrow$ vijolična

$\lambda = 440 - 509 \Rightarrow$ modra

$\lambda = 510 - 579 \Rightarrow$ zelena

$\lambda = 580 - 599 \Rightarrow$ rumena

$\lambda = 600 - 619 \Rightarrow$ oranžna

$\lambda = 620 - 645 - 779 \Rightarrow$ rdeča

$\lambda = 780 - \infty \Rightarrow$ infrardeča

Zrcala in leče:

-Ravno zrcalo – slika je navidezna in

nastane na drugi strani zrcala na enaki

razdalji kot predmet, kjer se sekajopodaljški

žarkov

-Zbiralno zrcalo – vbočeno – predmet

preslika v sliko

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{f} = \frac{2}{r} \Rightarrow f = \frac{r}{2}$$

-Razpršilno zrcalo – slika je vedno navidezna, pokončna in pomanjšana, ker se nahaja na drugi strani zrcala

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{f} = -\frac{2}{|r|} \Rightarrow f = -\frac{|r|}{2}$$

-Zbiralna leča – r(r') – slika je na drugi strani pomanjšana in obrnjena, ter pokončna

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{f} > \frac{1}{f} = (n-1) \left(\frac{1}{r} + \frac{1}{r'} \right) \rightarrow$$

-Razpršilna leča – r(r') – veljajo iste enačbe kot za zbiralno lečo