

**Fourierjeva vrsta na intervalu  $[-a, a]$ :**

$$f(x) = a_0 + \sum_{n=1}^{\infty} \left( a_n \cos \frac{n\pi x}{a} + b_n \sin \frac{n\pi x}{a} \right)$$

Koeficienti:

$$a_0 = \frac{1}{2a} \int_{-a}^a f(x) dx$$

$$a_n = \frac{1}{a} \int_{-a}^a f(x) \cos \frac{n\pi x}{a} dx$$

$$b_n = \frac{1}{a} \int_{-a}^a f(x) \sin \frac{n\pi x}{a} dx$$

Fourierjeva vrsta sode funkcije s periodo  $2a$ :

$$a_0 + \sum_{n=1}^{\infty} a_n \cos \frac{n\pi x}{a}$$

Koeficienti:

$$a_0 = \frac{1}{a} \int_0^a f(x) dx$$

$$a_n = \frac{2}{a} \int_0^a f(x) \cos \frac{n\pi x}{a} dx$$

**Fourierjeva formula (integral):**

$$f(x) = \frac{1}{\pi} \int_0^{\infty} [A(\omega) \cos \omega x + B(\omega) \sin \omega x] d\omega$$

Koeficienti:

$$A(\omega) = \int_{-\infty}^{\infty} f(t) \cos \omega t dt$$

$$B(\omega) = \int_{-\infty}^{\infty} f(t) \sin \omega t dt$$

Fourierjev integral sode funkcije:

$$f(x) = \frac{1}{\pi} \int_0^{\infty} A(\omega) \cos \omega x dx$$

Koeficienti:

$$A(\omega) = 2 \int_0^{\infty} f(t) \cos \omega t dt$$

**Taylorjeva vrsta v okolici točke  $a$ :**

$$f(x) = \sum_{n=0}^m \frac{f^{(n)}(a)}{n!} (x-a)^n + R_m$$

Ostane vrste:

$$R_m(x) = \sum_{n=m+1}^{\infty} a_n (x-a)^n$$

Ocena ostanka vrste:

$$R_m(x) = \frac{f^{(m+1)}(\xi)}{(m+1)!} (x-a)^{m+1}$$

Fourierjeva vrsta lihe funkcije s periodo  $2a$ :

$$\sum_{n=1}^{\infty} b_n \sin \frac{n\pi x}{a}$$

Koeficienti:

$$b_n = \frac{2}{a} \int_0^a f(x) \sin \frac{n\pi x}{a} dx$$

$$\omega = \frac{n\pi}{a}$$

Fourierjev integral lihe funkcije:

$$f(x) = \frac{1}{\pi} \int_0^{\infty} B(\omega) \sin \omega x dx$$

Koeficienti:

$$B(\omega) = 2 \int_0^{\infty} f(t) \sin \omega t dt$$