

SPROŠČANJE IN PRENOS TOPLOTE V BIOPROCESIH

Sproščanje toplote pri reakcijah

Pri reakciji sproščena ali absorbirana toplota je enaka razliki entalpij reaktantov in produktov:

$$\Delta H_r = \sum_{\text{produkti}} Mh - \sum_{\text{reaktanti}} Mh$$

M ... masa (kg)
 h ... specifična entalpija (J/kg)

Toplota zgorevanja: Δh_c (J/kg) ali (J/mol)

Standardna toplota zgorevanja (pri 25°C, 1 atm): Δh_c° (J/kg) ali (J/mol)

Dogovor: $\Delta h_c^\circ = 0$ za produkte oksidacij, kot so CO₂ (g), N₂, H₂O (l),
za ostale produkte je vselej $\Delta h_c^\circ < 0$

Standardna toplota reakcije:

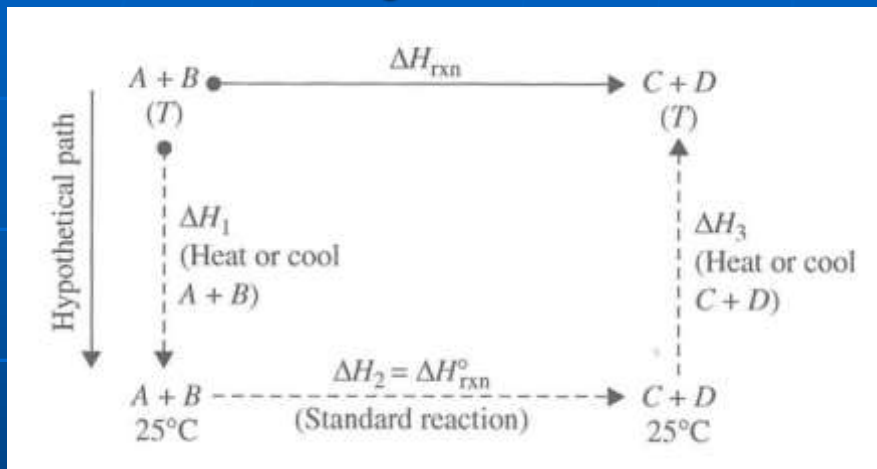
$$\Delta H_r^\circ = \sum_{\text{reaktanti}} n\Delta h_c^\circ - \sum_{\text{produkti}} n\Delta h_c^\circ$$

TABLE C.8 Heats of Combustion (Continued)

Compound	Formula	Molecular weight	State	Heat of combustion Δh_c (kJ g mol ⁻¹)
Alanine (L-)	C ₃ H ₇ O ₂ N	89.094	c	-1576.9
			g	-1715.0
Ammonia	NH ₃	17.03	g	-382.6
Ammonium ion	NH ₄ ⁺			-383
Arginine (D-)	C ₆ H ₁₄ O ₂ N ₄	174.203	c	-3738.4
Asparagine (L-)	C ₄ H ₈ O ₃ N ₂	132.119	c	-1928.0
Aspartic acid (L-)	C ₄ H ₇ O ₄ N	133.104	c	-1601.1
Benzaldehyde	C ₇ H ₆ O	106.124	l	-3525.1
			g	-3575.4
Butanoic acid	C ₄ H ₈ O ₂	88.106	l	-2183.6
			g	-2241.6
1-Butanol	C ₄ H ₁₀ O	74.123	l	-2675.9
			g	-2728.2
2-Butanol	C ₄ H ₁₀ O	74.123	l	-2660.6
			g	-2710.3
Butyric acid	C ₄ H ₈ O ₂	88.106	l	-2183.6
			g	-2241.6
Caffeine	C ₈ H ₁₀ O ₂ N ₄		s	-4246.5*
Carbon	C	12.011	c	-393.5
Carbon monoxide	CO	28.010	g	-283.0
Citric acid	C ₆ H ₈ O ₇		s	-1962.0
Codeine	C ₁₈ H ₂₁ O ₃ N·H ₂ O		s	-9745.7*
Cytosine	C ₄ H ₅ ON ₃	111.103	c	-2067.3
Ethane	C ₂ H ₆	30.070	g	-1560.7
Ethanol	C ₂ H ₆ O	46.069	l	-1366.8
			g	-1409.4
Ethylene	C ₂ H ₄	28.054	g	-1411.2
Ethylene glycol	C ₂ H ₆ O ₂	62.068	l	-1189.2
			g	-1257.0
Formaldehyde	CH ₂ O	30.026	g	-570.7
Formic acid	CH ₂ O ₂	46.026	l	-254.6
			g	-300.7
Fructose (D-)	C ₆ H ₁₂ O ₆		s	-2813.7
Fumaric acid	C ₄ H ₄ O ₄	116.073	c	-1334.0
Galactose (D-)	C ₆ H ₁₂ O ₆		s	-2805.7
Glucose (D-)	C ₆ H ₁₂ O ₆		s	-2805.0
Glutamic acid (L-)	C ₅ H ₉ O ₄ N	147.131	c	-2244.1
Glutamine (L-)	C ₅ H ₁₀ O ₃ N ₂	146.146	c	-2570.3
Glutaric acid	C ₅ H ₈ O ₄	132.116	c	-2150.9
Glycerol	C ₃ H ₈ O ₃	92.095	l	-1655.4
			g	-1741.2
Glycine	C ₂ H ₅ O ₂ N	75.067	c	-973.1
Glycogen	(C ₆ H ₁₀ O ₅) _x per kg		s	-17,530.1*
Guanine	C ₅ H ₅ ON ₅	151.128	c	-2498.2
Hexadecane	C ₁₆ H ₃₄	226.446	l	-10,699.2
			g	-10,780.5
Hexadecanoic acid	C ₁₆ H ₃₂ O ₂	256.429	c	-9977.9
			l	-10,031.3
			g	-10,132.3
Histidine (L-)	C ₆ H ₉ O ₂ N ₃	155.157	c	-3180.6
Hydrogen	H ₂	2.016	g	-285.8
Hydrogen sulphide	H ₂ S	34.08		-562.6
Inositol	C ₆ H ₁₂ O ₆		s	-2772.2*
Isoleucine (L-)	C ₆ H ₁₃ O ₂ N	131.175	c	-3581.1
Isoquinoline	C ₉ H ₇ N	129.161	l	-4686.5
Lactic acid (D,L-)	C ₃ H ₆ O ₃		l	-1368.3
Lactose	C ₁₂ H ₂₂ O ₁₁		s	-5652.5
Leucine (D-)	C ₆ H ₁₃ O ₂ N	131.175	c	-3581.7
Leucine (L-)	C ₆ H ₁₃ O ₂ N	131.175	c	-3581.6
Lysine	C ₆ H ₁₄ O ₂ N ₂	146.189	c	-3683.2
Malic acid (L-)	C ₄ H ₆ O ₅		s	-1328.8
Malonic acid	C ₃ H ₄ O ₄		s	-861.8
Maltose	C ₁₂ H ₂₂ O ₁₁		s	-5649.5
Mannitol (D-)	C ₆ H ₁₄ O ₆		s	-3046.5*
Methane	CH ₄	16.043	g	-890.8
Methanol	CH ₄ O	32.042	l	-726.1
			g	-763.7

Toplota reakcije pri nestandardnih pogojih

- reakcija $A+B \longrightarrow C+D$



$$\Delta H_r(\text{pri } T) = \Delta H_1 + \Delta H_r^\circ + \Delta H_3$$

- Primer: $C_6H_{12}O_6 + 6 O_2 \longrightarrow 6 CO_2 + 6 H_2O$

$$\Delta H_r(\text{pri } 37^\circ C) = -2801,7 \text{ kJ}$$

$$\Delta H_r^\circ = -2805,0 \text{ kJ}$$

Razliko lahko zanemarimo

Toplota reakcije za procese s proizvodnjo biomase

Termodinamika rasti celic:



Vsebnost energije organskih spojin je sorazmerna njihovi stopnji redukcije:

$$\Delta h_c^\circ = -q \cdot \gamma \cdot x_C$$

Δh_c° molarna toplota zgorevanja pri standardnih pogojih

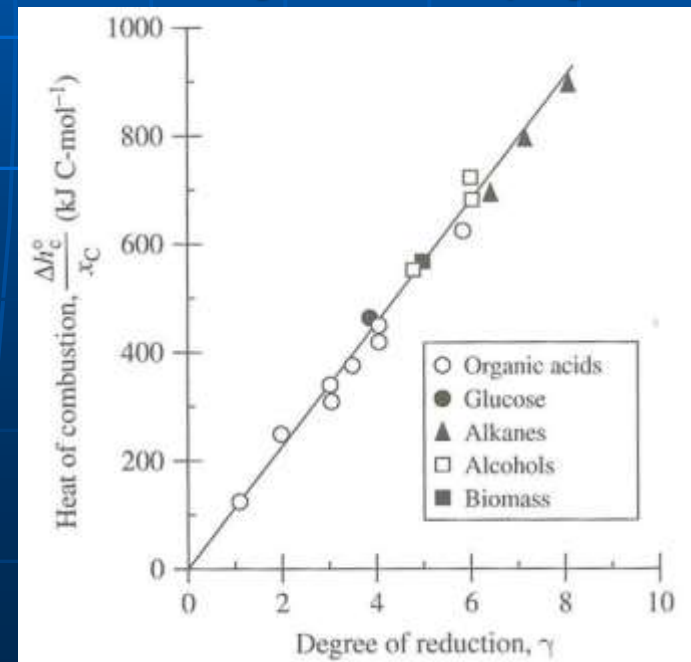
q Energija sproščena na mol prostih elektronov

γ stopnja redukcije spojine glede na N_2

x_C število atomov C v molekuli

Številne kemijske in biokemijske spojine, tudi biomasa:

$$q = 115 \text{ kJ/mol}$$



Toplota reakcije s kisikom kot akceptorjem e^-

Ker je stopnja redukcije neposredno povezana s količino kisika, potrebnega za popolno zgorenje, sta tudi Δh_c° in ΔH_r sorazmerna porabi O_2 .

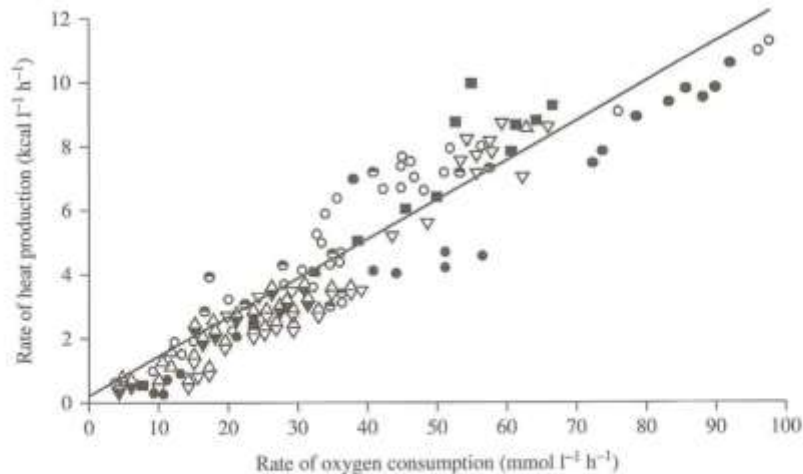


FIGURE 5.8 Correlation between rate of heat evolution and rate of oxygen consumption for a variety of microbial fermentations. (○) *Escherichia coli*, glucose medium; (◐) *Candida intermedia*, glucose medium; (△) *Candida intermedia*, molasses medium; (▽) *Bacillus subtilis*, glucose medium; (■) *B. subtilis*, molasses medium; (●) *B. subtilis*, soybean meal medium; (◑) *Aspergillus niger*, glucose medium; (●) *Asp. niger*, molasses medium. C.L. Cooney, D.J.C. Wang, and R.I. Mateles, *Measurement of heat evolution and correlation with oxygen consumption in microbial growth*, *Biotechnol. Bioeng.* 11, 269–281; Copyright © 1968. Reprinted by permission of John Wiley.

$$\Delta H_r \approx -460 \text{ kJ/mol } O_2$$

Če je vsa toplota na račun rasti, potem je: $\dot{Q} = -\Delta H_r$

$$\dot{Q} = (460 \text{ kJ/mol}) \cdot r_{O_2} \cdot V$$

$$U \cdot A \cdot \Delta T = (460 \text{ kJ/mol}) q_{O_2} \cdot X \cdot V$$

Če je ΔT max, potem:

$$X_{\max} = \frac{U A (T_F - T_{hv})}{460 \frac{\text{kJ}}{\text{mol}} q_{O_2} V}$$

Toplota reakcije z drugimi akceptorji e⁻



Če je vir N NH₃:

$$\Delta H^\circ_r = (n \Delta h^\circ_c)_{\text{substrat}} + (n \Delta h^\circ_c)_{\text{NH}_3} - (n \Delta h^\circ_c)_{\text{biomasa}} - (n \Delta h^\circ_c)_{\text{produkt}}$$

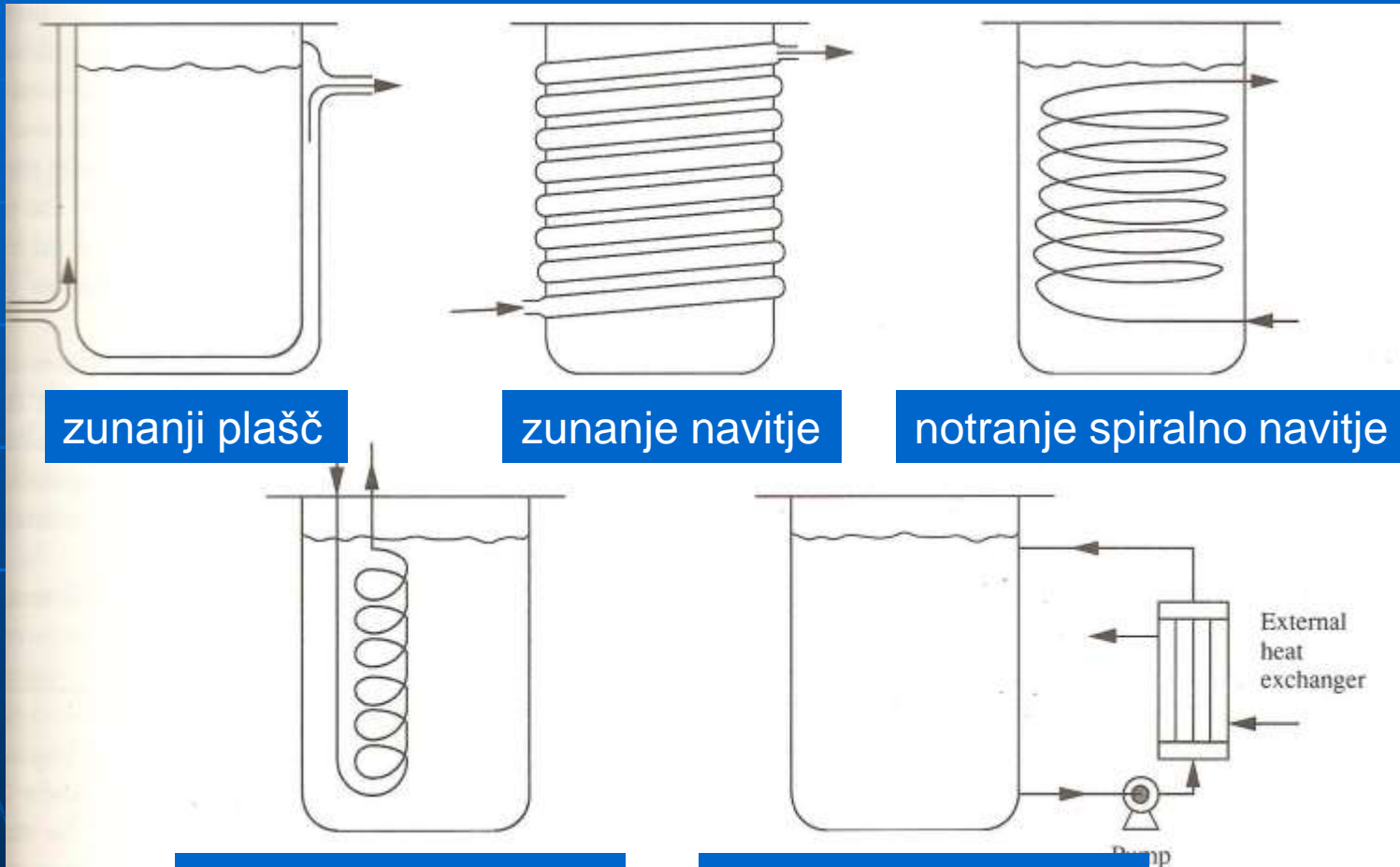
TABLE 5.1 Heats of Combustion of Bacteria and Yeast

Organism	Substrate	Δh_c (kJ g ⁻¹)
BACTERIA		
<i>Escherichia coli</i>	glucose	-23.04 ± 0.06
	glycerol	-22.83 ± 0.07
<i>Enterobacter cloacae</i>	glucose	-23.22 ± 0.14
	glycerol	-23.39 ± 0.12
<i>Methylophilus methylotrophus</i>	methanol	-23.82 ± 0.06
<i>Bacillus thuringiensis</i>	glucose	-22.08 ± 0.03
YEAST		
<i>Candida lipolytica</i>	glucose	-21.34 ± 0.16
<i>Candida boidinii</i>	glucose	-20.14 ± 0.18
	ethanol	-20.40 ± 0.14
	methanol	-21.52 ± 0.09
<i>Kluyveromyces fragilis</i>	lactose	-21.54 ± 0.07
	galactose	-21.78 ± 0.10
	glucose	-21.66 ± 0.19
	glucose*	-21.07 ± 0.07
		-21.30 ± 0.10
	-20.66 ± 0.26	
	-21.22 ± 0.14	

*Chemostat rather than batch culture: dilution rates were 0.036 h⁻¹, 0.061 h⁻¹, 0.158 h⁻¹, and 0.227 h⁻¹, respectively.

From J.-L. Cordier, B.M. Butsch, B. Birou, and U. von Stockar, 1987, The relationship between elemental composition and heat of combustion of microbial biomass, Appl. Microbiol. Biotechnol. 25: 305-312.

Oprema za gretje/hlajenje



zunanji plašč

zunanje navitje

notranje spiralno navitje

notranje navitje v obliki tuljave

zunanji toplotni menjalnik

TOPLOTNA BILANCA ZA HLADNEJŠI MEDIJ

$$\Phi_m \cdot c_p \cdot (T_{h,2} - T_{h,1}) = U \cdot A \cdot \Delta T_{\ln}$$

LOGARITEMSKA SREDNJA
TEMPERATURNNA RAZLIKA

$$\Delta T_{\ln} = \frac{(T_{p,1} - T_{h,1}) - (T_{p,2} - T_{h,2})}{\ln \frac{T_{p,1} - T_{h,1}}{T_{p,2} - T_{h,2}}}$$

Površina za hlajenje

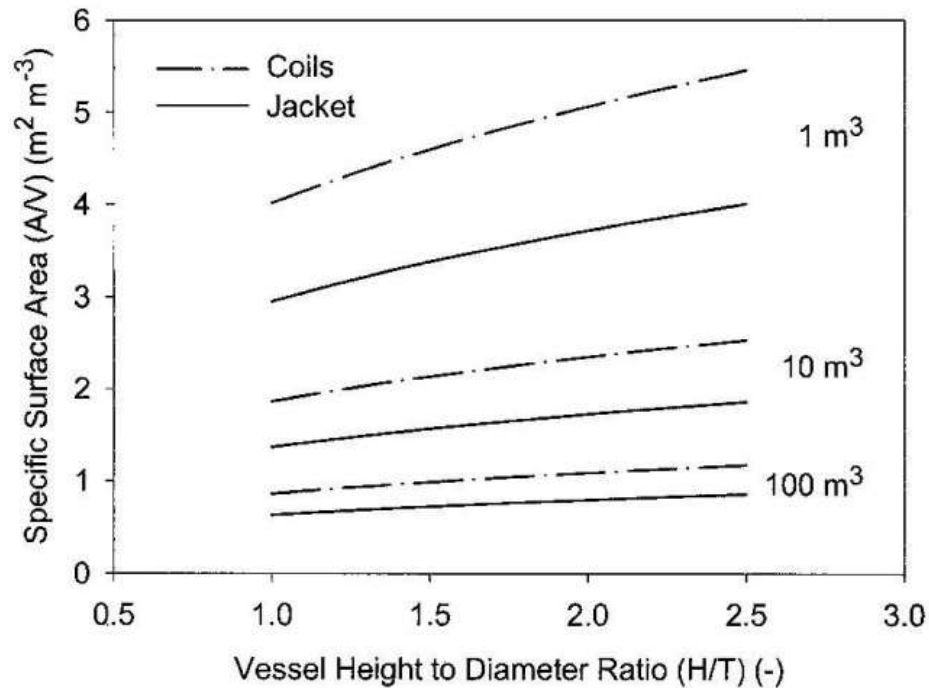
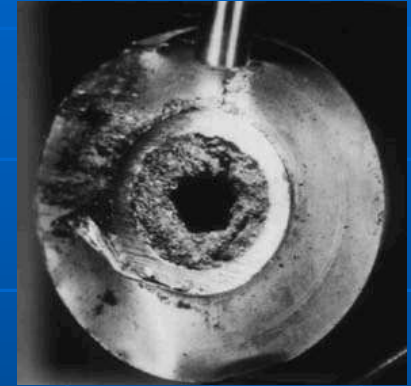


Figure 7. Variation of specific surface area with aspect ratio and scale for external jackets and internal coils. Data: Jacket and coils extend over 80% of height. Coils: $D_c = T/30$; Pitch = $2D_c$; Wall clearance = $2D_c$.

POVPREČNI KOEFICIENT TOPLOTNEGA PREHODA

$$\frac{1}{U} = \frac{1}{h_z} + \frac{1}{h_{fz}} + \frac{l_s}{\lambda_s} + \frac{1}{h_{fn}} + \frac{1}{h_n}$$



plast (biološka, korozija, karbonat...) na notranji površini menjalnika – angl. fouling

h_z ...koeficient toplotnega prestopa na strani brozge [W/m² K]

h_{fz} ...koeficient toplotnega prestopa na strani brozge, v plasti na zunanji strani cevi [W/m² K]

λ_s ...prevodnost stene [W/m K]

l_s ... debelina stene [m]

h_{fn} ...koeficient toplotnega prestopa v plasti v notranjosti cevi [W/m² K]

h_n ...koeficient toplotnega prestopa na strani brozge [W/m² K]

Odvisnost lokalne vrednosti koeficienta snovnega prestopa na strani brozge od razdalje od mešala

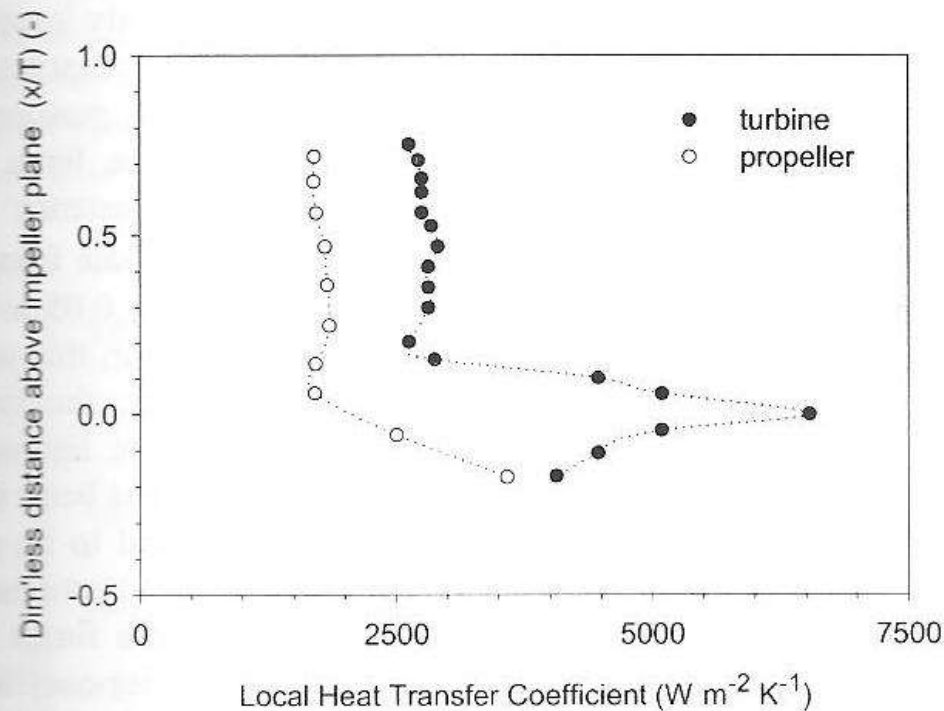


Figure 2. Variation of local heat transfer coefficients with axial position for turbine and propeller impellers, $D/T = 1/3$, $N = 0.5 s^{-1}$ (Man *et al.*, 1984).

Naloga

Bioreaktor prostornine 150 m^3 , kjer proizvajamo biomaso iz glukoze, deluje pri $35 \text{ }^\circ\text{C}$. Kultura porablja kisik s hitrostjo $1,5 \text{ kg/m}^3\text{h}$; mešalo oddaja 1 kW/m^3 energije. Hladilna voda iz bližnje reke, ki ima $10 \text{ }^\circ\text{C}$, prehaja skozi notranjo cev v fermentorju s hitrostjo $60 \text{ m}^3/\text{h}$. Če sistem deluje v stacionarnem stanju in če ni izparevanja, kakšna je temperatura vode na izstopu?

$$c_p \text{ vode} = 4190 \text{ J/kg K} \quad \text{oz.} \quad 75,4 \text{ J/mol K}$$

$$\rho \text{ vode} = 1000 \text{ kg/m}^3$$

Odgovor: $T = 25 \text{ }^\circ\text{C}$