

# Ekonometrija 1

## Enajste vaje:

### ***Konstantnost variance slučajne spremenljivke in heteroskedastičnost. Odsotnost koreliranosti slučajne spremenljivke in avtokorelacija.***

Na enajstih vajah bomo nadaljevali z obravnavo homoskedastičnosti kot ene temeljnih predpostavk klasičnega linearnega regresijskega modela. Spoznali bomo dva dodatna testa za preverjanje te predpostavke, tj. Breusch–Paganov in Whiteov test ter dodaten postopek ocenjevanja regresijskih modelov v primeru heteroskedastičnosti. Nato pa bomo obravnavali še eno temeljnih predpostavk klasičnega linearnega regresijskega modela, in sicer predpostavko o odsotnosti avtokorelacije.



**Primer 1:** Na podlagi podatkov za 50 ameriških zveznih držav za leto 1985 ocenite naslednjo funkcijo porabe bencina (glej datoteko `bencin.dta`):

$$CON_i = \beta_1 + \beta_2 REGMV_i + \beta_3 TAX_i + u_i.$$

Pri tem imajo posamezne spremenljivke naslednji pomen:

- ◆ *CON*: poraba bencina v posamezni državi (v milijonih sodčkov);
  - ◆ *REGMV*: število registriranih motornih vozil (v tisočih);
  - ◆ *TAX*: stopnja trošarine za bencin (v centih na galono).
- a) Opravite Breusch–Paganov test prisotnosti heteroskedastičnosti in pojasnite vaše ugotovitve. S pomočjo metode PNK–TNK zapišite model v obliki, ki bo zagotavljala, da je predpostavka o homoskedastičnosti ponovno izpolnjena in to tudi dokažite. Ocenite ta model, nato pa zapišite ustrezne (NENALICE) ocene prvotnega regresijskega modela.
  - b) Opravite Whiteov test prisotnosti heteroskedastičnosti in pojasnite vaše ugotovitve. S pomočjo metode PNK–TNK zapišite model v obliki, ki bo zagotavljala, da je predpostavka o homoskedastičnosti ponovno izpolnjena in to tudi dokažite. Ocenite ta model, nato pa zapišite ustrezne (NENALICE) ocene prvotnega regresijskega modela.
  - c) Poskušajte odpraviti ugotovljeno prisotnost heteroskedastičnosti še s pomočjo logaritemske transformacije spremenljivk. Ste bili pri tem uspešni?
  - d) Nazadnje s pomočjo Huber/White robustne cenilke variance izračunajte nepristranske standardne napake ocen parametrov. Katero predpostavko klasičnega linearnega regresijskega modela ste pri tem sprostili in kako?

**Izpis rezultatov obdelav v programskem paketu Stata:**

**. regress con regmv tax**

Source	SS	df	MS	Number of obs =	50
Model	19504553.9	2	9752276.93	F( 2, 47) =	152.36
Residual	3008446.64	47	64009.5029	Prob > F =	0.0000
				R-squared =	0.8664
				Adj R-squared =	0.8607
Total	22513000.5	49	459448.99	Root MSE =	253

con	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
regmv	.1861319	.0117189	15.88	0.000	.1625565 .2097074
tax	-53.59101	16.85588	-3.18	0.003	-87.50067 -19.68134
_cons	551.688	186.2709	2.96	0.005	176.9592 926.4168

**. predict econ, resid**  
**. gen econ2=econ^2**

**. \* Breusch-Paganov test**

**. sum econ2**

Variable	Obs	Mean	Std. Dev.	Min	Max
econ2	50	60168.93	207477.4	60.18166	1365618

**. regress econ2 regmv tax**

Source	SS	df	MS	Number of obs =	50
Model	5.9199e+11	2	2.9600e+11	F( 2, 47) =	9.17
Residual	1.5173e+12	47	3.2283e+10	Prob > F =	0.0004
				R-squared =	0.2807
				Adj R-squared =	0.2500
Total	2.1093e+12	49	4.3047e+10	Root MSE =	1.8e+05

econ2	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
regmv	23.26149	8.322487	2.80	0.007	6.518812 40.00418
tax	-29576.46	11970.63	-2.47	0.017	-53658.25 -5494.665
_cons	284600.5	132284.9	2.15	0.037	18477.51 550723.5

**. display invchi2tail(2,0.05)**  
5.9914645

**. display chi2tail(2,81.774988)**  
1.749e-18

**. qui regress con regmv tax**  
**. estat hettest regmv tax**

Breusch-Pagan / Cook-Weisberg test for heteroskedasticity

Ho: Constant variance

Variables: regmv tax

chi2(2) = **81.76**  
Prob > chi2 = **0.0000**

```
. qui regress econ2 regmv tax
. predict econ2fit, xb
. inspect econ2fit
```

```
econ2fit: Linear prediction
-----
|          #          Negative      Total   Integers   Nonintegers
|          #          Zero          -       -         -
|          #          Positive     36      -         36
|          #          Total        50      1         49
|          #          Missing      -
+-----+-----+
-111465.5      416881.8      50
(50 unique values)
```

```
. gen lecon2=log(econ2)
. qui regress lecon2 regmv tax
. predict lecon2fit, xb

. gen td=sqrt(exp(lecon2fit))

. gen cont=con/td
. gen regmvt=regmv/td
. gen taxt=tax/td
. gen kt=1/td

. regress cont regmvt taxt kt, nocons
```

Source	SS	df	MS	Number of obs =	50
Model	1590.87775	3	530.292582	F( 3, 47) =	204.85
Residual	121.6675	47	2.58867021	Prob > F =	0.0000
Total	1712.54525	50	34.2509049	R-squared =	0.9290
				Adj R-squared =	0.9244
				Root MSE =	1.6089

cont	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
regmvt	.1628148	.0108746	14.97	0.000	.140938 .1846916
taxt	-20.32982	8.020062	-2.53	0.015	-36.4641 -4.195536
kt	253.5014	95.08184	2.67	0.010	62.22145 444.7814

```
. gen contfit=_b[regmvt]*regmv+_b[taxt]*tax+_b[kt]

. correlate con contfit
(obs=50)
```

	con	contfit
con	1.0000	
contfit	0.9261	1.0000

```
. scalar r2p=r(rho)^2
. display r2p
.85758636

. drop econ2fit td cont regmvt taxt kt contfit lecon2 lecon2fit
```

```
. * Whiteov test
```

```
. gen regmv2=regmv^2
. gen tax2=tax^2
. gen regmvtax=regmv*tax
```

```
. regress econ2 regmv tax regmv2 tax2 regmvtax
```

Source	SS	df	MS	Number of obs =	50
Model	1.4017e+12	5	2.8033e+11	F( 5, 44) =	17.43
Residual	7.0764e+11	44	1.6083e+10	Prob > F =	0.0000
				R-squared =	0.6645
				Adj R-squared =	0.6264
Total	2.1093e+12	49	4.3047e+10	Root MSE =	1.3e+05

econ2	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
regmv	140.5628	39.92468	3.52	0.001	60.09989 221.0257
tax	-237873	103340.2	-2.30	0.026	-446141.4 -29604.56
regmv2	-.0005147	.00106	-0.49	0.630	-.002651 .0016216
tax2	12346.99	4688.527	2.63	0.012	2897.89 21796.1
regmvtax	-12.84508	3.60418	-3.56	0.001	-20.10883 -5.58133
_cons	1098291	556502.1	1.97	0.055	-23265.35 2219847

```
. scalar theta=e(N)*e(r2)
```

```
. display theta, invchi2tail(e(rank)-1,0.05), chi2tail(e(rank)-1,theta)
33.22564 11.070498 3.394e-06
```

```
. qui regress con regmv tax
. estat imtest, white
```

White's test for Ho: homoskedasticity  
against Ha: unrestricted heteroskedasticity

```
chi2(5) = 33.23
Prob > chi2 = 0.0000
```

Cameron & Trivedi's decomposition of IM-test

Source	chi2	df	p
Heteroskedasticity	33.23	5	0.0000
Skewness	13.51	2	0.0012
Kurtosis	1.57	1	0.2095
Total	48.31	8	0.0000

```
. qui regress econ2 regmv tax regmv2 tax2 regmvtax
. predict econ2fit, xb
. inspect econ2fit
```

econ2fit: Linear prediction

		Number of Observations		
		Total	Integers	Nonintegers
#	Negative	23	-	23
#	Zero	-	-	-
#	Positive	27	-	27
#	Total	50	-	50
#	Missing	-	-	-
-98912.37 1020180		50		
(50 unique values)				

```
. gen lecon2=log(econ2)
. qui regress lecon2 regmv tax regmv2 tax2 regmvtax
. predict lecon2fit, xb
```

```
. gen td=sqrt(exp(lecon2fit))
```

```
. gen cont=con/td  
. gen regmvt=regmv/td  
. gen taxt=tax/td  
. gen kt=1/td
```

```
. regress cont regmvt taxt kt, nocons
```

Source	SS	df	MS	Number of obs =	50
Model	2201.7405	3	733.913501	F( 3, 47) =	286.87
Residual	120.240758	47	2.55831399	Prob > F =	0.0000
				R-squared =	0.9482
				Adj R-squared =	0.9449
Total	2321.98126	50	46.4396252	Root MSE =	1.5995

cont	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
regmvt	.1662324	.009169	18.13	0.000	.1477868 .184678
taxt	-24.70128	10.15112	-2.43	0.019	-45.12271 -4.279852
kt	286.102	110.0896	2.60	0.012	64.63024 507.5738

```
. gen contfit=_b[regmvt]*regmv+_b[taxt]*tax+_b[kt]
```

```
. correlate con contfit  
(obs=50)
```

	con	contfit
con	1.0000	
contfit	0.9274	1.0000

```
. scalar r2p=r(rho)^2  
. display r2p  
.86002384
```

```
. drop econ2fit td cont regmvt taxt kt contfit lecon2 lecon2fit
```

```
. * Logaritemska transformacija spremenljivk
```

```
. gen lcon=log(con)  
. gen lregmv=log(regmv)  
. gen ltax=log(tax)
```

```
. regress lcon lregmv ltax
```

Source	SS	df	MS	Number of obs =	50
Model	38.3992068	2	19.1996034	F( 2, 47) =	253.25
Residual	3.56316785	47	.075812082	Prob > F =	0.0000
				R-squared =	0.9151
				Adj R-squared =	0.9115
Total	41.9623747	49	.856374993	Root MSE =	.27534

lcon	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
lregmv	.8796717	.0415988	21.15	0.000	.7959857 .9633578
ltax	-.649004	.1747917	-3.71	0.001	-1.00064 -.2973685
_cons	.7274507	.555704	1.31	0.197	-.3904817 1.845383

```
. estat hettest lregmv ltax
```

```
Breusch-Pagan / Cook-Weisberg test for heteroskedasticity
Ho: Constant variance
Variables: lregmv ltax
```

```
chi2(2)      =    21.25
Prob > chi2  =    0.0000
```

```
. estat imtest, white
```

```
White's test for Ho: homoskedasticity
against Ha: unrestricted heteroskedasticity
```

```
chi2(5)      =    13.61
Prob > chi2  =    0.0183
```

```
Cameron & Trivedi's decomposition of IM-test
```

Source	chi2	df	p
Heteroskedasticity	13.61	5	0.0183
Skewness	1.34	2	0.5109
Kurtosis	2.05	1	0.1525
Total	17.00	8	0.0301

```
. * Uporaba robustnih standardnih napak
```

```
. regress con regmv tax, robust
```

```
Linear regression
```

```
Number of obs =    50
F( 2, 47) =    41.10
Prob > F      =    0.0000
R-squared     =    0.8664
Root MSE     =    253
```

con	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]
regmv	.1861319	.021533	8.64	0.000	.1428132 .2294507
tax	-53.59101	23.8975	-2.24	0.030	-101.6666 -5.515436
_cons	551.688	237.1574	2.33	0.024	74.58876 1028.787

**Primer 2:** Na podlagi četrtletnih podatkov za ZDA za obdobje 1976q1–1990q4 ocenite naslednjo funkcijo povpraševanja po novih avtomobilih (glej datoteko avtotrg.dta):

$$AVTOP_t = \beta_1 + \beta_2 CENA_t + \beta_3 RRDP_t + \beta_4 OM_t + u_t.$$

Pri tem imajo posamezne spremenljivke naslednji pomen:

- ◆ *AVTOP*: število prodanih novih avtomobilov na 1.000 prebivalcev;
- ◆ *CENA*: indeks cen novih avtomobilov (1982q1=100);
- ◆ *RRDP*: realni razpoložljivi dohodek na prebivalca (v 1.000 USD);
- ◆ *OM*: referenčna obrestna mera pri poslovnih bankah (v %).

Najprej s pomočjo grafične metode odkrivanja avtokorelacije preverite, ali je v zgornji funkciji povpraševanja po novih avtomobilih mogoče zaznati prisotnost avtokorelacije prvega in četrtega reda. Grafično preverite tudi morebitne znake slabe specifikacije modela. Nato opravite še Durbin–Watsonov  $d$ -test. Pri tem ocenite tudi koeficient avtokorelacije prvega in četrtega reda (na različne načine). Pojasnite vaše ugotovitve.

***Izpis rezultatov obdelav v programskem paketu Stata:***

```
. tsset kvartal
      time variable: kvartal, 1976q1 to 1990q4
                delta: 1 quarter
```

```
. regress avtop cena rrdp om
```

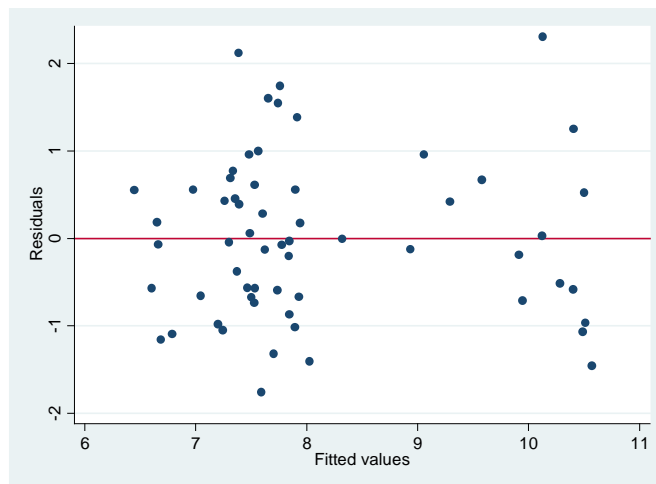
Source	SS	df	MS	Number of obs =	60
Model	85.0940388	3	28.3646796	F( 3, 56) =	31.69
Residual	50.1162514	56	.894933061	Prob > F =	0.0000
Total	135.21029	59	2.29169983	R-squared =	0.6293
				Adj R-squared =	0.6095
				Root MSE =	.94601

avtop	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
cena	-.1062054	.0200516	-5.30	0.000	-.1463737 -.0660371
rrdp	1.241812	.4282211	2.90	0.005	.3839823 2.099642
om	-.1344411	.042009	-3.20	0.002	-.2185954 -.0502869
_cons	7.012139	3.027984	2.32	0.024	.9463581 13.07792

```
. predict eavto, resid
```

```
. * Analiza prisotnosti avtokorelacije - Graficna metoda
```

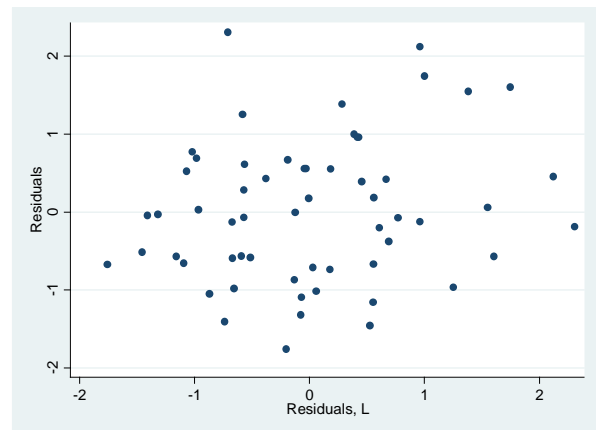
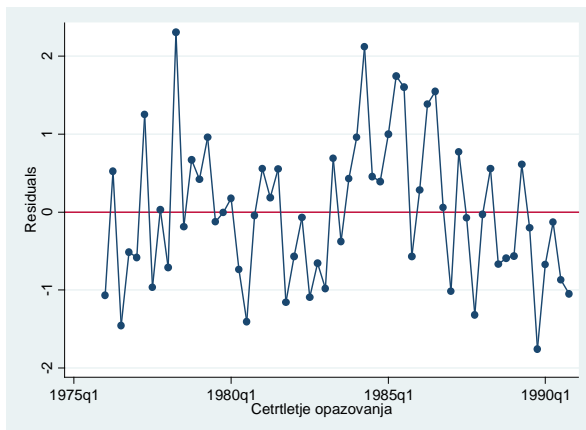
```
. rvfplot, yline(0)
```



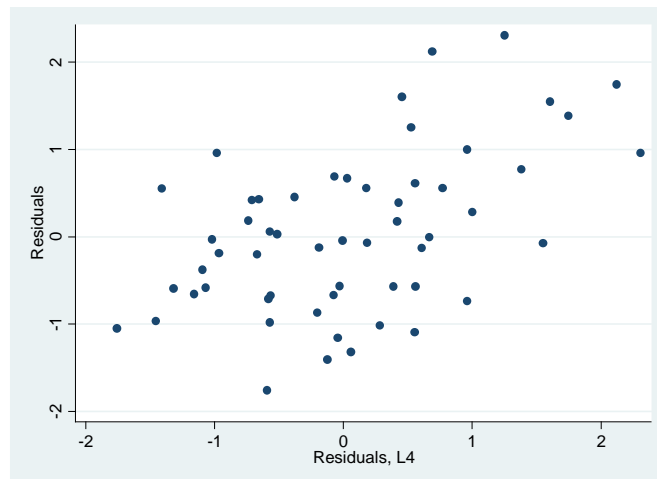
```
. gen eavto1=eavto[_n-1]
(1 missing value generated)
```

```
. gen eavto4=eavto[_n-4]
(4 missing values generated)
```

```
. twoway connected eavto kvartal, yline(0) . scatter eavto l.eavto
```



```
. scatter eavto l4.eavto
```



```
. * Analiza prisotnosti avtokorelacije - Ocenjevanje koeficienta AK 1. reda
```

```
. gen eeavtott1=eavto*eavto1
(1 missing value generated)

. qui sum eeavtott1, detail
. scalar rhostevec=r(N)*r(mean)

. gen eavto2=eavto^2
. qui sum eavto2, detail
. scalar rhoimenoalec1=r(N)*r(mean)

. scalar rhoapprox1=rhostevec/rhoimenoalec1

. display rhostevec, rhoimenoalec1, rhoapprox1
9.4984437 50.116252 .18952821
```

```
. corrgram eavto
```

LAG	AC	PAC	Q	Prob>Q	-1	0	1	-1	0	1
					[Autocorrelation]			[Partial Autocor]		
1	0.1895	0.1935	2.2648	0.1323						
2	0.1233	0.0937	3.2397	0.1979						
3	0.1002	0.0692	3.8949	0.2730						



4	0.4777	0.4853	19.056	0.0008	---	---
5	0.0258	-0.1839	19.102	0.0018		
6	-0.0894	-0.2036	19.653	0.0032		
7	-0.0759	-0.0910	20.057	0.0054		
8	0.1829	0.0772	22.45	0.0041		
9	-0.1178	-0.1764	23.462	0.0052		
10	-0.1922	-0.0379	26.209	0.0035		

```
. gen eavto12=eavto1^2
(1 missing value generated)

. qui sum eavto12, detail
. scalar rhoimenoalec2=r(N)*r(mean)

. scalar rhoapprox2=rhostevec/rhoimenoalec2

. display rhostevec, rhoimenoalec2, rhoapprox2
9.4984437 49.011816 .19379906
```

```
. regress eavto eavto1, nocons
```

Source	SS	df	MS	Number of obs =	59
Model	1.84078945	1	1.84078945	F( 1, 58) =	2.27
Residual	47.1365277	58	.812698753	Prob > F =	0.1378
				R-squared =	0.0376
				Adj R-squared =	0.0210
Total	48.9773171	59	.830124019	Root MSE =	.9015

eavto	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
eavto1	.1937991	.1287699	1.51	0.138	-.0639619 .45156

```
. scalar rho=_b[eavto1]
. display rho
.19379906
```

**\* Analiza prisotnosti avtokorelacije - Durbin-Watsonov d-test**

```
. gen eavtott12=(eavto-eavto1)^2
(1 missing value generated)

. qui sum eavtott12, detail
. scalar dwstevec=r(N)*r(mean)

. qui sum eavto2, detail
. scalar dwimenoalec=r(N)*r(mean)

. scalar dw=dwstevec/dwimenoalec
. display dwstevec, dwimenoalec, dw
78.992245 50.116252 1.5761802
```

```
. qui regress avtop cena rrdp om
. estat dwatson
```

Durbin-Watson d-statistic( 4, 60) = 1.57618

**\* Analiza prisotnosti avtokorelacije - Ocenjevanje koeficienta AK 4. reda**

```
. gen eeavtott4=eavto*eavto4
(4 missing values generated)
```

```

. qui sum eavtott4, detail
. scalar rhostevec=r(N)*r(mean)

. qui sum eavto2, detail
. scalar rhoimenoalec1=r(N)*r(mean)

. scalar rhoapprox1=rhostevec/rhoimenoalec1

. display rhostevec, rhoimenoalec1, rhoapprox1
23.94273 50.116252 .47774381

```

```

. corrgram eavto

```

LAG	AC	PAC	Q	Prob>Q	-1	0	1	-1	0	1
					[Autocorrelation]			[Partial	Autocor]	
1	0.1895	0.1935	2.2648	0.1323		-		-		
2	0.1233	0.0937	3.2397	0.1979						
3	0.1002	0.0692	3.8949	0.2730						
4	0.4777	0.4853	19.056	0.0008		---		---		
5	0.0258	-0.1839	19.102	0.0018						
6	-0.0894	-0.2036	19.653	0.0032						
7	-0.0759	-0.0910	20.057	0.0054						
8	0.1829	0.0772	22.45	0.0041		-				
9	-0.1178	-0.1764	23.462	0.0052						
10	-0.1922	-0.0379	26.209	0.0035		-				

```

. gen eavto42=eavto4^2
(4 missing values generated)

. qui sum eavto42, detail
. scalar rhoimenoalec2=r(N)*r(mean)

. scalar rhoapprox2=rhostevec/rhoimenoalec2

. display rhostevec, rhoimenoalec2, rhoapprox2
23.94273 47.781433 .50108856

```

```

. regress eavto eavto4, nocons

```

Source	SS	df	MS	Number of obs = 56		
Model	11.9974278	1	11.9974278	F( 1, 55) =	19.23	
Residual	34.3161111	55	.623929294	Prob > F =	0.0001	
				R-squared =	0.2590	
				Adj R-squared =	0.2456	
Total	46.313539	56	.827027482	Root MSE =	.78989	

eavto	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
eavto4	.5010886	.1142715	4.39	0.000	.2720833	.7300939

```

. scalar rho=_b[eavto4]
. display rho
.50108856

```

