

1. naloga: pokaži delno pravilnost

$$\{y > 3\}$$

$$x := 2 \cdot y;$$

$$\{y > 3, x = 2 \cdot y\} \quad \text{CSP in EQ}$$

$$x := x - y$$

$$\{y > 3, x = y\} \quad \text{AS}$$

$$\{x > 3\}$$

ker so cela št.

$$\{x \geq 4\}$$

Za popolno pravilnost bi namesto CSP uporabili CST.

2. naloga: pokaži delno pravilnost

{ true }

if  $x < y$  then

{  $x < y$  }

$z := x$

{  $x < y, z = x$  }  $\Rightarrow$  {  $z = \min(x, y)$  }

CSP, EQ  
[CST]

else:

{  $x \geq y$  }

$z := y$

{  $x \geq y, z = y$  }  $\Rightarrow$  {  $z = \min(x, y)$  }

CSP, EQ  
[CST]

CD

3. naloga: pokaži popolno pravilnost

$$[a=0 \wedge y=0 \wedge a \leq b]$$

$$I \Leftrightarrow y = a \cdot x \wedge 0 \leq a \leq b$$

[I]

while  $a < b$  do (  $\underbrace{e}$  )

$$[y = a \cdot x \wedge 0 \leq a \leq b \wedge a < b \wedge b - a = n]$$

$$a := a + 1;$$

$$[y = (a-1) \cdot x \wedge 0 \leq a-1 \leq b \wedge a-1 < b \wedge b - a + 1 = n] \quad AS$$

$$y := y + x$$

$$[y - x = (a-1) \cdot x \wedge 0 \leq a-1 \leq b \wedge a-1 < b \wedge b - a + 1 = n] \quad AS$$

$$[y = a \cdot x \wedge 0 \leq a \leq b \wedge b - a = n - 1 < n]$$

done

$$[y = a \cdot x \wedge 0 \leq a \leq b \wedge b \leq a]$$

$$[y = x \cdot b]$$

WHT

4. naloga: pokaži popolno pravilnost

$$[x \geq 0]$$

$$y := 0; z := x$$

$$[x \geq 0, y = 0, z = x] \quad \text{EQ, EQ}$$

$$\text{while } z - y > 1 \text{ do}$$

$$[y^2 \leq x \leq z^2 \wedge 0 \leq y \leq z \leq x \wedge z - y > 1 \wedge z - y = \text{NV}]$$

$$s := (y + z) / 2;$$

$$[y^2 \leq x \leq z^2 \wedge 0 \leq y \leq z \leq x \wedge z - y > 1 \wedge z - y = \text{NV} \wedge s = (y + z) / 2] \quad \text{EQ}$$

if  $s \cdot s < x$  then

$$[-II-, s^2 < x]$$

$$y := s$$

$$[(2y - z)^2 \leq x \leq z^2 \wedge 0 \leq 2y - z \leq z \wedge z - 2y - z > 1 \wedge z - 2y + z = \text{NV} \wedge y^2 < x] \quad \text{AS}$$

else  $[-II-, s^2 \geq x]$   $z := s$

$$[y^2 \leq x \leq (2z - y)^2 \wedge 0 \leq y \leq 2z - y \leq x \wedge 2z - y - y > 1 \wedge 2z - y - y = \text{NV} \wedge z^2 \geq x] \quad \text{AS}$$

$$[y^2 \leq x \leq z^2 \wedge 0 \leq y \leq z \leq x \wedge z - y < \text{NV}] \quad \text{CD (sledi iz končnih pogojev obeh vej stavka if)}$$

$$[y^2 \leq x \leq z^2 \wedge 0 \leq y \leq z \leq x \wedge z - y \leq 1] \quad \text{WHT} \implies [y^2 \leq x \leq (y + 1)^2]$$

$$I \Leftrightarrow y^2 \leq x \leq z^2 \wedge 0 \leq y \leq z \leq x$$

$$e = z - y$$

$$2s - z = y$$

$$2s - y = z$$