

Formule za višjo trdnost

$\vec{p}_i \cdot \vec{n}_j = p_j \cdot n_i$		
$P_{x1} = \sigma_x \cdot n_{x1} + \tau_{xy} \cdot n_{y1}$ $P_{y2} = \tau_{yx} \cdot n_{x1} + \sigma_y \cdot n_{y1}$	$P_i = \sigma_{ij} \cdot n_j$	
Glavne normalne nap. $(\sigma_x - \sigma) \cdot n_x + \tau_{xy} \cdot n_y = 0$ $\tau_{yx} \cdot n_x + (\sigma_y - \sigma) \cdot n_y = 0$	$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$	$\tau_{n,i} = \sqrt{P_i^2 - \sigma_{n,i}^2}$
$\sigma_n = \frac{\sigma_x + \sigma_y}{2} + \frac{\sigma_x - \sigma_y}{2} \cdot \cos(2\varphi) + \tau_{xy} \cdot \sin(2\varphi)$		
$\tau_n = \frac{\sigma_y - \sigma_x}{2} \cdot \sin(2\varphi) + \tau_{xy} \cdot \cos(2\varphi)$		$n_{i,x}^2 + n_{i,y}^2 + n_{i,z}^2 = 1$
$\tau_{\max} = \frac{\sigma_2 - \sigma_1}{2}$		$\sigma_x + \sigma_y = \sigma_1 + \sigma_2$
Deformacije (lega in velikost)		
$\tan \varphi = \frac{n_x}{n_y} \quad \vec{n} = (n_x, n_y)$		
Hookov zakon		
$\mu = \frac{E}{2(1+\nu)} = G$	$\epsilon_{xx} = \frac{1}{E} [\sigma_x - \nu(\sigma_y + \sigma_z)]$	$\epsilon_{xy} = \frac{1+\nu}{E} \cdot \tau_{xy} = \frac{1}{2} \gamma_{xy}$
	$\epsilon_{yy} = \frac{1}{E} [\sigma_y - \nu(\sigma_z + \sigma_x)]$	$\epsilon_{yz} = \frac{1+\nu}{E} \cdot \tau_{yz} = \frac{1}{2} \gamma_{yz}$
$\epsilon_{n,AB} = \frac{\Delta AB}{AB}$	$\epsilon_{zz} = \frac{1}{E} [\sigma_z - \nu(\sigma_x + \sigma_y)]$	$\epsilon_{zx} = \frac{1+\nu}{E} \cdot \tau_{zx} = \frac{1}{2} \gamma_{zx}$
$\epsilon_n = \epsilon_{xx} \cdot \cos^2(\varphi) + \epsilon_{yy} \cdot \sin^2(\varphi) + \epsilon_{xy} \cdot \sin(2\varphi)$		
$\frac{1}{2} \gamma_n = \frac{\epsilon_{yy} - \epsilon_{xx}}{2} \cdot \sin(2\varphi) + \epsilon_{xy} \cdot \cos(2\varphi)$	$\epsilon_{1,2} = \frac{\epsilon_x + \epsilon_y}{2} \pm \sqrt{\left(\frac{\epsilon_x - \epsilon_y}{2}\right)^2 + \epsilon_{xy}^2}$	
$\left(\frac{1}{2} \gamma_n\right)^2 = \epsilon^2 - \epsilon_n^2$	$\gamma_{1,2} = \pm(\epsilon_1 - \epsilon_2)$	
$\vec{n}_2 = (\cos(\alpha_2), \cos(\beta_2), \cos(\gamma_2))$	$\tan(2\varphi) = \frac{2 \cdot \epsilon_{xy}}{\epsilon_{xx} - \epsilon_{yy}}$	

Virtualno delo	Airy-eva funkcija
$\delta W_n = \delta W_z$	RNS: $\Delta \Delta F - (1-\nu) \Delta V = 0$

$$\delta W_n = \int_s \left[\frac{N \cdot \delta N}{E \cdot A} + \chi \frac{T \cdot \delta T}{G \cdot A} + \frac{M \cdot \delta M}{E \cdot I} \right] ds$$

$$\delta W_z = \sum_i (\delta F_i \cdot u_i + \delta M_i \cdot \varphi_i)$$

$$u_G + u_V = 0 \text{ ali } u_G + u_V + \Delta L = 0$$

$$\Delta L = \frac{N \cdot L}{E \cdot A} + \alpha \cdot \Delta T \cdot L$$

$$\text{RNS: } \sigma_z = 0; \varepsilon_{zz} \neq 0$$

$$\sigma_r = A + B \cdot r^{-2} - \frac{3+\nu}{8} \cdot \rho \cdot \omega^2 \cdot r^2$$

$$\sigma_\varphi = A - B \cdot r^{-2} - \frac{1+3\nu}{8} \cdot \rho \cdot \omega^2 \cdot r^2$$

$$u_r = \frac{r}{E} \left[(1-\nu) \cdot A - (1+\nu) \cdot B \cdot r^{-2} - \frac{1-\nu^2}{8} \cdot \rho \cdot \omega^2 \cdot r^2 \right] + \alpha \cdot \Delta T \cdot r$$

$$\varepsilon_{zz} = \frac{\partial u_z}{\partial z} \quad u_z = \frac{\nu \cdot z}{E} \left[\frac{1+\nu}{2} \cdot \rho \cdot \omega^2 \cdot r^2 - 2A \right] + \alpha \cdot \Delta T \cdot r$$

$$\text{RDS: } \sigma_z \neq 0; \varepsilon_{zz} = 0$$

$$\sigma_r = A + B \cdot r^{-2} - \frac{3-2\nu}{8(1-\nu)} \cdot \rho \cdot \omega^2 \cdot r^2$$

$$\sigma_\varphi = A + B \cdot r^{-2} - \frac{1+2\nu}{8(1-\nu)} \cdot \rho \cdot \omega^2 \cdot r^2$$

$$\sigma_z = 2 \cdot \nu \cdot A - \frac{\nu}{2(1-\nu)} \cdot \rho \cdot \omega^2 \cdot r^2 - \alpha \cdot \Delta T \cdot E$$

$$u_r = \frac{(1+\nu)r}{E} \left[(1-2\nu) \cdot A - B \cdot r^{-2} - \frac{1-2\nu}{8(1-\nu)} \cdot \rho \cdot \omega^2 \cdot r^2 \right] + (1+\nu)\alpha \cdot \Delta T \cdot r$$

$$\text{RDS: } \Delta \Delta F - \frac{(1-2\nu)}{(1-\nu)} \Delta V = 0$$

Če je $\Delta V = 0$ je RNS = RDS

$$\frac{\partial^4 F}{\partial x^4} + 2 \frac{\partial^4 F}{\partial x^2 \partial y^2} + \frac{\partial^4 F}{\partial y^4} = 0$$

$$\sigma_x = \frac{\partial^2 F}{\partial y^2} - V; \quad \sigma_y = \frac{\partial^2 F}{\partial x^2} - V; \quad \tau_{xy} = -\frac{\partial^2 F}{\partial x \partial y}$$

Krožne stene v el. plastičnem področju:

$$\text{RNS: } \sigma_r \neq 0, \sigma_\varphi \neq 0, \sigma_z = 0, \tau_{r\varphi} = 0$$

TRESCA

$$\left[(\sigma_r - \sigma_\varphi)^2 - \sigma_0^2 \right] \cdot \left[\sigma_\varphi^2 - \sigma_0^2 \right] \cdot \left[\sigma_r^2 - \sigma_0^2 \right] = 0$$

$$1) \quad \sigma_r = \sigma_\varphi = \pm \sigma_0; \quad \sigma_r' = \pm \sigma_0 \cdot \ln(C/r); \quad \sigma_\varphi' = \pm \sigma_0 \cdot (\ln(C/r) + 1)$$

$$u_r^{pl} = \pm \frac{(1-\nu)}{E} \cdot \sigma_0 \cdot r \cdot \ln(C/r) + \frac{D}{r} + \alpha \cdot \Delta T \cdot r$$

$$2) \quad \sigma_r = \sigma_\varphi; \quad \sigma_r' = \pm \sigma_0 + C/r$$

$$u_r^{pl} = \pm \frac{(1-\nu)}{E} \cdot (\pm \sigma_0 \cdot r + C) + \frac{D}{r} + \alpha \cdot \Delta T \cdot r$$

$$3) \quad \sigma_r = \sigma_\varphi; \quad \sigma_r' = \pm \sigma_0 = \sigma_\varphi'; \quad u_r^{pl} = \pm \frac{(1-\nu) \cdot r \cdot \sigma_0}{E} + \frac{D}{r} + \alpha \cdot \Delta T \cdot r$$

