

3. DOMAČA NALOGA

3.1 Določi definicijska območja in skiciraj grafe funkcij

$$\begin{aligned}f_1(x) &= x^3 - 9x^2, \\f_2(x) &= 4x - 4x^2 - x^3, \\f_3(x) &= (-x^2 + 4x - 4)^{\frac{1}{4}}, \\f_4(x) &= (\sin(x))^{\frac{1}{3}}, \\f_5(x) &= (\cos(x))^{\frac{1}{4}}, \\f_6(x) &= 2 \cos(3x) - 1, \\f_7(x) &= -\sin(2x + \pi), \\f_8(x) &= 2 \operatorname{tg}(x/4), \\f_9(x) &= \exp(2x + 1) + 3, \\f_{10}(x) &= \exp(|x|) - 2, \\f_{11}(x) &= \log(|x| + 1), \\f_{12}(x) &= 2 \log(x) + 1, \\f_{13}(x) &= \log(x^3 - 9x^2).\end{aligned}$$

3.2 Izračunaj naslednje limite.

$$\begin{aligned}\lim_{x \rightarrow 0} \frac{\sin(7x)}{x}, \\ \lim_{x \rightarrow 0} \frac{\sin(7x) \sin(8x)}{x^2}, \\ \lim_{x \rightarrow 0} \frac{\sin(7x) \sin(8x) \sin(9x)}{x^3}, \\ \lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 2x - 2} - \sqrt{x^2 + 2}}{x - 2}, \\ \lim_{x \rightarrow 3} \frac{\sqrt{x^2 + 3x - 3} - \sqrt{x^2 + 6}}{x - 3}, \\ \lim_{x \rightarrow 4} \frac{\sqrt{x^2 + 2x - 4} - \sqrt{x^2 + 4}}{x - 4},\end{aligned}$$

$$\lim_{x \rightarrow 5} \frac{\sqrt{x^2 + 3x} - \sqrt{x^2 + 15}}{x - 5},$$

$$\lim_{x \rightarrow \infty} \sqrt{x^2 + 3x - 3} - \sqrt{x^2 + 6},$$

$$\lim_{x \rightarrow \infty} \frac{5^{4x-3} - 3x + 2x^3}{4 \cdot 5^{4x+1} + 2x^4},$$

$$\lim_{x \rightarrow \infty} \frac{7^{2x} - 5x + 6x^6}{8 \cdot 7^{2x+4} + 2x^5},$$

$$\lim_{x \rightarrow \infty} (x^3 + x^2 + 3)e^{-2x},$$

$$\lim_{x \rightarrow \infty} \frac{4^{5x-3} - 2x + 3x^2}{3 \cdot 4^{5x-1} + 3x^3},$$

$$\lim_{x \rightarrow \infty} \left(1 + \frac{13}{3 + 3x^2}\right)^{3x^2+5},$$

$$\lim_{x \rightarrow \infty} \left(1 + \frac{3x - 4}{5x + 2x^2}\right)^{2x+2},$$

$$\lim_{x \rightarrow \infty} \left(1 + \frac{x + 3}{2 + 4x^2}\right)^{5x-2}.$$